Stability

The roots $s_i$ will determine if the overall system is BIBO stable.

Assume we have a causal LTI system. The solution to our differential equation is of the form

$$y(t) = y_c(t) + y_p(t)$$

where $y_c(t)$ is the steady-state solution and $y_p(t)$ is the transient solution.